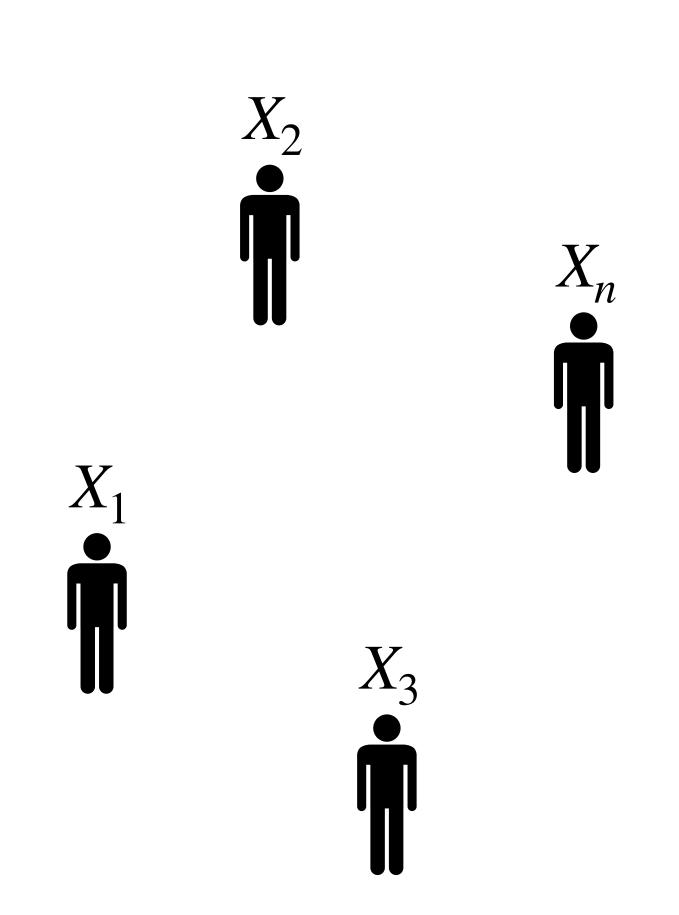
Asymptotic Statistics: Introduction

M2RI - Toulouse University

Author: Clément Lalanne

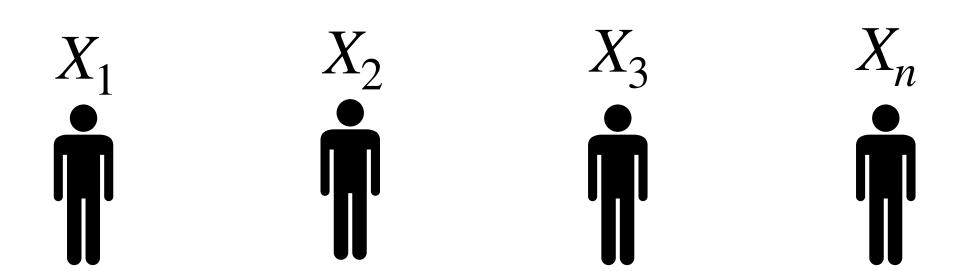
Objectives



$$X_1, X_2, \dots, X_n \stackrel{\text{i.i.d.}}{\sim} \mathscr{L}_{\theta_0}$$

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When can we write $\hat{\theta} \approx \theta_0$?

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Strong law of large numbers :
$$\frac{1}{n} \sum_{i=1}^{n} X_i \xrightarrow[n \to \infty]{\text{p.s.}} \mu := \mathbb{E}(X_1)$$

Central limit theorem :
$$\sqrt{n}\left(\frac{1}{n}\sum_{i=1}^n X_i - \mu\right) \xrightarrow[n \to \infty]{\mathscr{L}} \mathcal{N}(0,\sigma^2 := Var(X_1))$$

Content

Random vectors

- Different convergences
- Fourier transform
- Asymptotic probabilistic notations

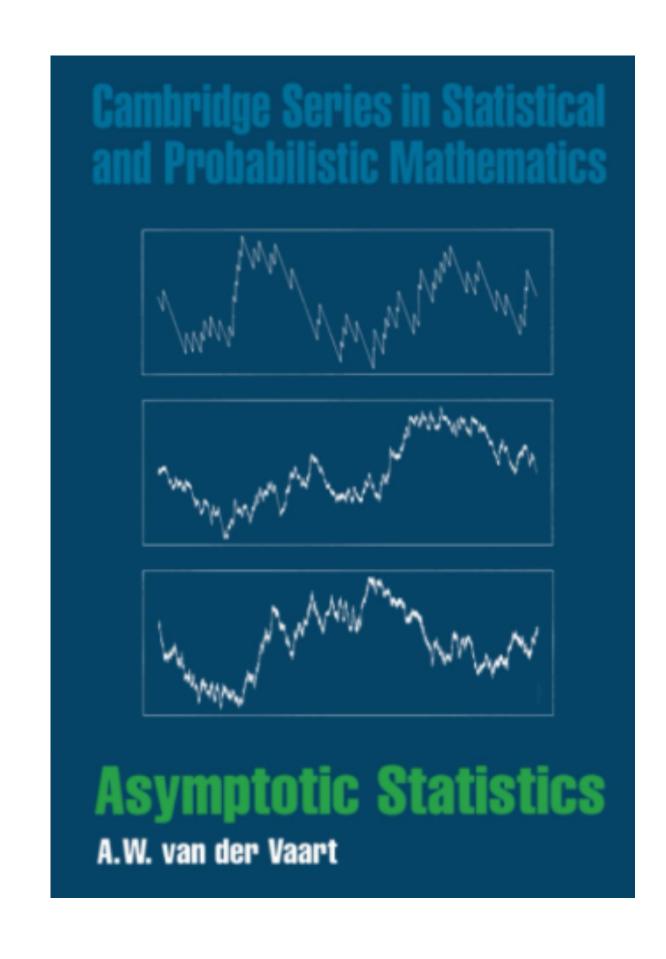
Tools for statistics

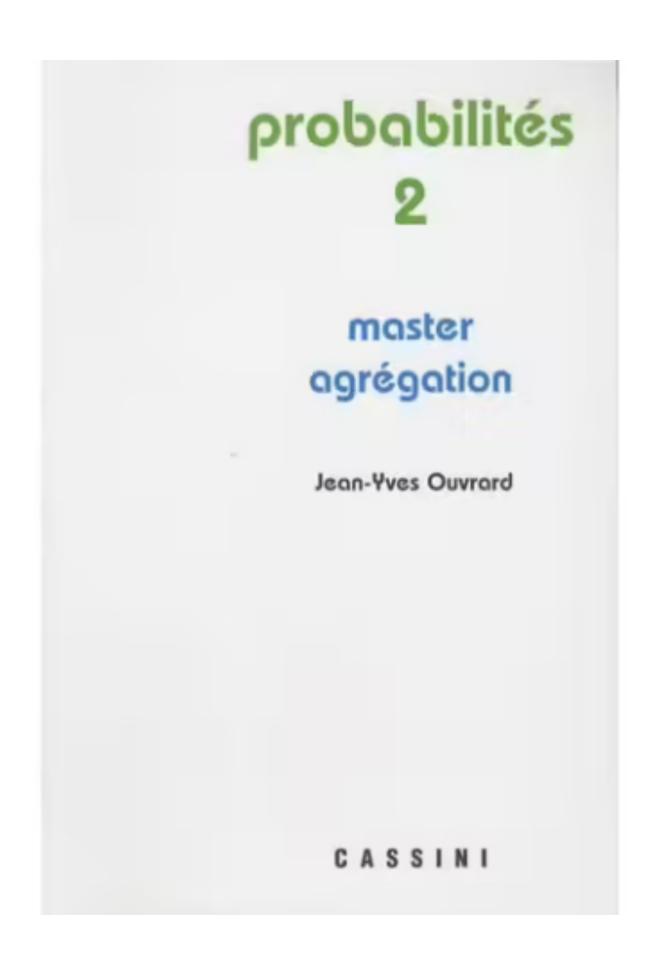
- Laws of large numbers
- Delta method
- Method of moments
- M and Z estimators

Empirical processes theory

- Uniform convergence
- Bracketing numbers
- Consistency of M and Z estimators
- Asymptotic normality

References





Page for the course



Clément Lalanne



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My work focuses on Machine Learning, Differential Privacy, Statistics and Optimization.

Teaching

- Assymptotic Statistics (M2 RI Toulouse University / ISAE Supaero) : ...
- Mathematical Methods for Supervised Learning (M1 SID Toulouse University): Course 2025-2026.
- Mathematics of Machine Learning (M2 MAPI3 Toulouse University): Course 2025-2026, Projects 2025-2026.
- Teaching Archive

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